## Unpacked South Dakota State Mathematics Standards

Purpose: In order for students to have the best chance of success, standards, assessment, curriculum resources, and instruction must be aligned in focus, coherence, and rigor. Unpacked standards documents are intended to help align instruction to the focus, coherence, and rigor of the South Dakota State Mathematics Standards. The standards have been organized in clusters as they are not so much built from topics, but rather woven out of progressions. Not all content in a given grade is emphasized equally in the mathematics standards. Some clusters require greater emphasis than others based on the depth of the ideas, the time that they take to master, and/or their importance to future mathematics or the demands of college and career readiness. To say that some things have greater emphasis is not to say that anything in the standards can safely be neglected in instruction. Neglecting standards will leave gaps in student skill and understanding and may leave students unprepared for the challenges of a later grade.

## Domain: Algebra

## Grade Level: Algebra 2

A2.A.REI.A Cluster: Understand Solving Equations as a Process of Reason and Explain the Reasoning
This cluster builds on the framework of solving equations and extends it to rational and radical equations (and the knowledge of extraneous solutions).
> **This is a SUPPORTING cluster. (It's not major since this standard is specific to rational and radical equations.) Students should spend the large majority of their time (65-85\%) on the major work of the grade. Supporting work and, where appropriate, additional work should be connected to and engage students in the major work of the grade.

> A2.A.REI.A. 2 Solve rational and radical equations in one variable, and give examples showing how extraneous solutions may arise. Rational functions are limited to those whose numerators are of degree at most 1 and denominators of degree at most 2. Radical functions are limited to square roots or cube roots of at most quadratic polynomials.

Aspects of Rigor for Students: (Conceptual, Procedural, and/or Application)

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| Conceptual Understanding | Procedural Fluency | Application |
| :--- | :--- | :--- |
| Learners understand the <br> mathematical process in solving <br> rational and radical equations. <br> Students are able to identify <br> extraneous solutions and explain why <br> they are extraneous given the context <br> of the problem. | Learners will solve radical and rational <br> equations and determine extraneous <br> solutions. |  |

## Enacting the Mathematical Practices - Evidence of Students Engaging in the Practices

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.

- Students explain in their own words why extraneous solutions arise.

4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.

- Students determine true solutions (not extraneous).

7. Look for and make use of structure.

| - Students recognize the structure of doing and undoing as a part of solving equations and inequalities. <br> 8. Look for and express regularity in repeated reasoning. |  |  |
| :---: | :---: | :---: |
| Vertical and Horizontal Coherence and Learning Progressions |  |  |
| Previous Learning Connections | Current Learning Connections | Future Learning Connections |
| In Algebra 1, students solved linear and quadratic equations. | In this course, students will extend their solving skills learned in Algebra 1 to rational and radical equations. Students will also relate the solving of other nonlinear equations learned in this course to solving rational and radical equations. | In future math classes students will solve more challenging nonlinear equations, including trigonometric equations. |
| Vocabulary (key terms and definitions) |  |  |
| - Extraneous Solution <br> - Radical Equation <br> - Rational Equation |  |  |
| Relevance, Explanations, and Examples: |  |  |
| Achievement Level Descriptors |  |  |
| Cluster: Understand Solving Equations as a Process of Reason and Explain the Reasoning |  |  |
| Concepts and Procedures | Level 1: Students should be able to explain solution steps for solving one-step linear equations in one variable. |  |
|  | Level 2: Students should be able to look for and make use of structure to solve simple radical equations and simple rational equations in one variable in which the variable term is in the numerator and should understand the solution steps as a process of reasoning. They should be able to understand and explain solution steps for solving linear equations in one variable as a process of reasoning. |  |
|  | Level 3: Students should be able to look for and make use of structure to solve simple radical and rational equations in one variable presented in various forms. They should be able to understand and explain solution steps for solving quadratic, radical, and rational equations in one variable as a process of reasoning. |  |
|  | Level 4: Students should be able to give examples showing how extraneous solutions may arise and why they arise when solving linear, quadratic, radical, and rational equations. |  |

