**4th Grade Level 1 Understanding**

**Domain #1**

**Operations and Algebraic Thinking**

* **Target A:** Use the four operations with whole numbers to solve problems.
  + Level 1 students should be able to use the four operations (add, subtract, multiply, and divide) to solve one-step problems involving equal groups and arrays.

**Number and Operations – Base Ten**

* **Target D:** Generalize place value understanding for multi- digit whole numbers.
  + Level 1 students should be able to read and write multi-digit whole numbers less than or equal to 1,000 using base-ten numerals, number names, and expanded form; compare multi-digit numbers up to 1,000 using <, >, and =; and round multi-digit whole numbers up to 1,000 to any place.
* **Target E:** Use place value understanding and properties of operations to perform multi- digit arithmetic.
  + Level 1 students should be able to add and subtract one- and two-digit whole numbers using strategies based on place value; multiply two one-digit whole numbers based on place value and properties of operations; and find whole-number quotients with no remainders with up to two-digit dividends and one- digit divisors using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division.

**Number and Operations – Fractions**

* **Target F:** Extend understanding of fraction equivalence and ordering.
  + Level 1 students should be able to recognize that fraction comparisons are valid only when the two fractions are referring to the same whole.
* **Target G:**  Build fractions from unit fractions by applying and extending previous understandings of operations on whole numbers.
  + Level 1 students should be able to understand that a fraction a/b with a > 1 is the sum of its unit fractional parts by extending previous understandings of addition on whole numbers. They should be able to identify fractions using visual models.

**Domain #2**

**Operations and Algebraic Thinking**

* **Target B:** Gain familiarity with factors and multiples.
  + Level 1 students should be able to recognize that a whole number is a multiple of each of its factors.
* **Target C:**  Generate and analyze patterns.
  + Level 1 students should be able to extend a number or shape pattern that follows a given rule.

**Measurement and Data**

* **Target I:** Solve problems involving measurement and conversion of measurements from a larger unit to a smaller unit.
  + Level 1 students should be able to know relative sizes of measurement units within one system of units, including km, m, cm; kg, g; lb., oz.; l, ml; and hr., min, sec.
* **Target J:** Represent and interpret data.
  + Level 1 students should be able to identify data from a given line plot using whole numbers.

**Geometry**

* **Target L:** Draw and identify lines and angles, and classify shapes by properties of their lines and angles.
  + Level 1 students should be able to draw points, lines, line segments, rays, angles (right, acute, obtuse), and perpendicular and parallel lines; recognize a line of symmetry for a familiar two-dimensional figure; and identify right triangles.

**4th Grade Level 2 Understanding**

**Domain #1**

**Operations and Algebraic Thinking**

**-Threshold:** The student who just enters Level 2 should be able to:

* Add and subtract to solve one-step problems involving an unknown number.
* **Target A:** Use the four operations with whole numbers to solve problems.
  + Level 2 students should be able to use the four operations to solve one-step problems involving an unknown number. They should be able to realize that it is appropriate to multiply or divide in order to solve familiar multiplicative comparison problems.

**Number and Operations – Base Ten**

**-Threshold:** The student who just enters Level 2 should be able to:

* Look for and use repeated reasoning to generalize place value understanding in order to read and write multi-digit whole numbers less than or equal to 100,000 using base-ten numerals and number names.
* Use place value understanding to add and subtract two- and three-digit whole numbers using a standard algorithm.
* **Target D:** Generalize place value understanding for multi- digit whole numbers.
  + Level 2 students should look for and use repeated reasoning to generalize place value understanding to be able to read and write multi-digit whole numbers less than or equal to 100,000 using base-ten numerals, number names, and expanded form; compare multi-digit numbers up to 100,000 using <,>, and =; and round multi-digit whole numbers up to 100,000 to any place.
* **Target E:** Use place value understanding and properties of operations to perform multi- digit arithmetic.
  + Level 2 students should be able to use place value understanding to add and subtract two- and three-digit whole numbers using a standard algorithm; multiply whole numbers up to and including four digits by one digit based on place value and properties of operations; find whole-number quotients and remainders with up to two-digit dividends and one-digit divisors using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division; and illustrate multiplication and division by using equations, arrays, and/or area models.

**Number and Operations – Fractions**

**-Threshold:** The student who just enters Level 2 should be able to:

* Recognize equivalent fractions using visual models.
* Use visual fraction models to represent a problem.
* Express a fraction with denominator 10 as an equivalent fraction with denominator 100.
* **Target F:** Extend understanding of fraction equivalence and ordering.
  + Level 2 students should be able to compare two fractions with different numerators and different denominators using <, >, and = by comparing to a benchmark fraction such as 1/2 and recognize equivalent fractions using visual models.
* **Target G:**  Build fractions from unit fractions by applying and extending previous understandings of operations on whole numbers.
  + Level 2 students should be able to understand that a fraction a/b is a multiple of 1/b by extending previous understanding of multiplication on whole numbers; solve one-step problems involving addition and subtraction of fractions referring to the same whole with like denominators; and use visual fraction models and/or equations to represent the problem.
* **Target H:**  Understand decimal notation for fractions, and compare decimal fractions.
  + Level 2 students should be able to express a fraction with denominator 10 as an equivalent fraction with denominator 100 and express those fractions as decimals.

**Domain #2**

**Operations and Algebraic Thinking**

**-Threshold:** The student who just enters Level 2 should be able to:

* Determine whether a given whole number in the range of 1–100 is a multiple of a given one-digit number.
* Generate a shape pattern that follows a given rule.
* **Target B:** Gain familiarity with factors and multiples.
  + Level 2 students should be able to find factor pairs for whole numbers in the range of 1–100 that are multiples of 2 or 5 and determine whether a given whole number in the range of 1–100 is a multiple of a given one-digit number.
* **Target C:**  Generate and analyze patterns.
  + Level 2 students should be able to generate a number or shape pattern that follows a given rule.

**Measurement and Data**

**-Threshold:** The student who just enters Level 2 should be able to:

* Apply the perimeter formula to rectangles in mathematical problems.
* Use data from a given line plot using fractions 1/2, 1/4, and 1/8 to solve one-step problems.
* Recognize whole-number degrees on a protractor.
* **Target I:** Solve problems involving measurement and conversion of measurements from a larger unit to a smaller unit.
  + Level 2 students should be able to express measurements in a larger unit in terms of a smaller unit within a single system of measurement, record measurement equivalents in a two-column table, and apply the perimeter formula to rectangles in mathematical problems.
* **Target J:** Represent and interpret data.
  + Level 2 students should be able to use data from a given line plot using fractions 1/2, 1/4, and 1/8 to solve one-step problems.
* **Target K:** Geometric measurement: understand concepts of angles and measure angles.
  + Level 2 students should be able to recognize whole-number degrees on a protractor and measure angles in whole-number degrees using a protractor.

**Geometry**

**-Threshold:** The student who just enters Level 2 should be able to:

* Identify points, lines, line segments, and rays.
* **Target L:** Draw and identify lines and angles, and classify shapes by properties of their lines and angles.
  + Level 2 students should be able to identify points, lines, line segments, rays, angles (right, acute, obtuse), and perpendicular and parallel lines in two- dimensional figures and recognize all lines of symmetry in unfamiliar two-dimensional figures.

**4th Grade Level 3 Understanding**

**Domain #1**

**Operations and Algebraic Thinking**

**-Threshold:** The student who just enters Level 3 should be able to:

* Multiply and divide to solve one-step problems involving equal groups or arrays.
* **Target A:** Use the four operations with whole numbers to solve problems.
  + Level 3 students should be able to use the four operations (add, subtract, multiply, and divide) to solve one-step problems involving equal groups and arrays, including problems where the remainder must be interpreted. They should be able to find an unknown number and represent problems using equations with a symbol representing the unknown quantity.

**Number and Operations – Base Ten**

**-Threshold:** The student who just enters Level 3 should be able to:

* Read and write multi-digit whole numbers less than or equal to 1,000,000 using base-ten numerals, number names, and expanded form.
* Multiply four-digit whole numbers by a one-digit number.
* **Target D:** Generalize place value understanding for multi- digit whole numbers.
  + Level 3 students should look for and use repeated reasoning to generalize place value understanding to be able to read and write multi-digit whole numbers less than or equal to 1,000,000 using base-ten numerals, number names, and expanded form; compare multi-digit numbers up to 1,000,000 using <,>, and =; round multi-digit whole numbers up to 1,000,000 to any place; and recognize that in a multi- digit whole number, a digit in one place represents ten times what it represents in the place to its right.
* **Target E:** Use place value understanding and properties of operations to perform multi- digit arithmetic.
  + Level 3 students should be able to fluently add and subtract multi-digit whole numbers using the standard algorithm; multiply whole numbers including two digits by two digits based on place value and properties of operations; find whole-number quotients and remainders with up to four-digit dividends and one- digit divisors using strategies based on place value understanding, the properties of operations, and/or the relationship between multiplication and division; and explain multiplication and division using equations, arrays, and/or area models.

**Number and Operations – Fractions**

**-Threshold:** The student who just enters Level 3 should be able to:

* Generate equivalent fractions using visual models.
* Identify and generate equivalent forms of a fraction with like denominators.
* Add two fractions with respective denominators 10 and 100.
* **Target F:** Extend understanding of fraction equivalence and ordering.
  + Level 3 students should be able to extend understanding to compare two fractions with different numerators and different denominators using <, >, and = by creating common denominators or numerators and recognize and generate equivalent fractions using visual models.
* **Target G:**  Build fractions from unit fractions by applying and extending previous understandings of operations on whole numbers.
  + Level 3 students should be able to identify and generate equivalent forms of a fraction including mixed numbers with like denominators and solve one-step problems involving multiplication of a fraction by a whole number.
* **Target H:** Understand decimal notation for fractions, and compare decimal fractions.
  + Level 3 students should be able to add two fractions with respective denominators 10 and 100 by first converting to two fractions with like denominators; compare two decimals to the hundredths using >, <, =, or on a number line; and compare decimals by reasoning about their size.

**Domain #2**

**Operations and Algebraic Thinking**

**-Threshold:** The student who just enters Level 3 should be able to:

* Find factor pairs for whole numbers in the range of 1–100.
* Identify apparent features of a pattern in a problem with scaffolding.
* **Target B:** Gain familiarity with factors and multiples.
  + Level 3 students should be able to find all factor pairs for whole numbers in the range of 1–100 and determine whether a given whole number in the range of 1–100 is prime or composite.
* **Target C:**  Generate and analyze patterns.
  + Level 3 students should be able to analyze a pattern for apparent features that are not explicit in the rule itself.

**Measurement and Data**

**-Threshold:** The student who just enters Level 3 should be able to:

* Represent measurement quantities using diagrams such as number line diagrams that feature a measurement scale.
* Interpret data from a line plot to solve problems involving addition of fractions with like denominators by using information presented in line plots.
* Construct angles between 0 and 180 degrees in whole-number degrees using a protractor.
* **Target I:** Solve problems involving measurement and conversion of measurements from a larger unit to a smaller unit.
  + Level 3 students should be able to use the four operations to solve problems involving distances, intervals of time, liquid volumes, masses of objects, and money, including problems involving simple fractions or decimals, and problems that require expressing measurements given in a larger unit in terms of a smaller unit; represent measurement quantities using diagrams such as number line diagrams that feature a measurement scale; and apply the area formula to rectangles in mathematical problems.
* **Target J:** Represent and interpret data.
  + Level 3 students should be able to create a line plot to represent a data set using fractions 1/2, 1/4, and 1/8 and interpret data from a line plot to solve problems involving addition and subtraction of fractions with like denominators.
* **Target K:** Geometric measurement: understand concepts of angles and measure angles.
  + Level 3 students should be able to construct angles in whole-number degrees using a protractor, use understanding of angle concepts to decompose a larger angle with two or more smaller angles that have the same sum as the original, and determine an unknown angle measure in a diagram.

**Geometry**

**-Threshold:** The student who just enters Level 3 should be able to:

* Draw lines of symmetry for two-dimensional figures.
* **Target L:** Draw and identify lines and angles, and classify shapes by properties of their lines and angles.
  + Level 3 students should be able to draw lines of symmetry for two-dimensional figures, classify two- dimensional figures based on parallel or perpendicular lines or angles of specified lines, and recognize right triangles as a category.

**4th Grade Level 4 Understanding**

**Domain #1**

**Operations and Algebraic Thinking**

**-Threshold:** The student who just enters Level 4 should be able to:

* Assess the reasonableness of answers using mental computation and estimation strategies, including rounding.
* **Target A:** Use the four operations with whole numbers to solve problems.
  + Level 4 students should be able to assess the reasonableness of answers using mental computation and estimation strategies, including rounding.

**Number and Operations – Fractions**

**-Threshold:** The student who just enters Level 4 should be able to:

* Compare two fractions with different numerators and different denominators using <, >, and =.
* Compare two decimals to the hundredths using <, >, and = or a number line and justify the conclusions by using visual models. Generate equivalent fractions using visual models.
* **Target F:** Extend understanding of fraction equivalence and ordering.
  + Level 4 students should be able to extend understanding to compare two fractions with different numerators and different denominators using <, >, and = and justify the conclusions using a visual fraction model.
* **Target H:** Understand decimal notation for fractions, and compare decimal fractions.
  + Level 4 students should be able to compare two decimals to the hundredths using <, >, and = and justify the conclusions by using visual models.

**Domain #2**

**Measurement and Data**

**-Threshold:** The student who just enters Level 4 should be able to:

* Apply the perimeter formula to rectangles in real-world problems.
* Solve addition problems to find unknown angles on a diagram in mathematical problems.
* **Target I:** Solve problems involving measurement and conversion of measurements from a larger unit to a smaller unit.
  + Level 4 students should be able to apply the perimeter and area formulas to rectangles in word problems.
* **Target K:** Geometric measurement: understand concepts of angles and measure angles.
  + Level 4 students should be able to solve addition and subtraction problems to find unknown angles on a diagram in problems by using an equation with a symbol for the unknown angle measure.